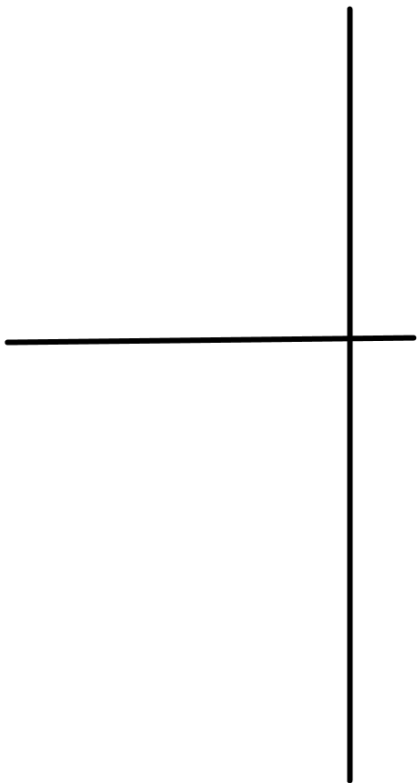
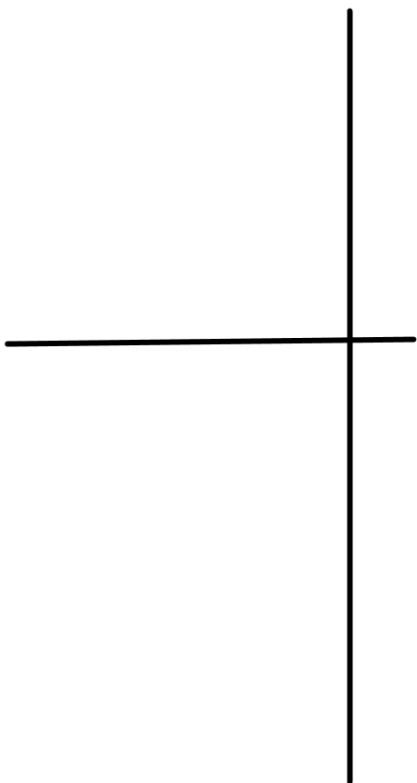


Two-Column Proof



Two-Column Proof



Complete the proof by giving the reason for the indicated step.

If $\frac{2}{3}x = 8 - 2x$, then $x = 3$.

Given: $\frac{2}{3}x = 8 - 2x$ Prove: $x = 3$

- \Rightarrow a. $\frac{2}{3}x = 8 - 2x$
b. $2x = 3(8 - 2x)$
c. $2x = 24 - 6x$
d. $8x = 24$
e. $x = 3$

- a. Substitution property of equality
b. Multiplication property of equality
c. Reflexive property of equality
d. Given

Complete the proof by giving the reason for the indicated step.

If $\frac{2}{3}x = 8 - 2x$, then $x = 3$.

Given: $\frac{2}{3}x = 8 - 2x$ Prove: $x = 3$

- \Rightarrow a. $\frac{2}{3}x = 8 - 2x$
b. $2x = 3(8 - 2x)$
c. $2x = 24 - 6x$
d. $8x = 24$
e. $x = 3$

- a. Distributive property
b. Multiplication property of equality
c. Associative property of equality
d. Commutative property of equality

Complete the proof by giving the reason for the indicated step.

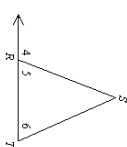
If $\frac{2}{3}x = 8 - 2x$, then $x = 3$.

Given: $\frac{2}{3}x = 8 - 2x$ Prove: $x = 3$

- $\frac{2}{3}x = 8 - 2x$
- $2x = 3(8 - 2x)$
- $2x = 24 - 6x$
- $8x = 24$
- $x = 3$

- Addition property of equality
- Division property of equality
- Symmetric property of equality
- Multiplication property of equality

Copy and complete the proof. Give the reason for the indicated step.

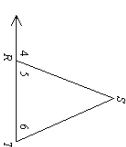


If $m\angle 4 + m\angle 6 = 180^\circ$, then $m\angle 5 = m\angle 6$.
Given: $m\angle 4 + m\angle 6 = 180^\circ$ Prove: $m\angle 5 = m\angle 6$

- $m\angle 4 + m\angle 6 = 180^\circ$
- $m\angle 4 + m\angle 5 = 180^\circ$
- $m\angle 4 + m\angle 5 = m\angle 4 + m\angle 6$
- $m\angle 4 = m\angle 4$
- $\angle 5 = \angle 6$

- Reflexive property of equality
- Substitution property of equality
- Given
- Addition property of equality

Copy and complete the proof. Give the reason for the indicated step.

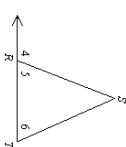


If $m\angle 4 + m\angle 6 = 180^\circ$, then $m\angle 5 = m\angle 6$.
Given: $m\angle 4 + m\angle 6 = 180^\circ$ Prove: $m\angle 5 = m\angle 6$

- $m\angle 4 + m\angle 6 = 180^\circ$
- $m\angle 4 + m\angle 5 = 180^\circ$
- $m\angle 4 + m\angle 5 = m\angle 4 + m\angle 6$
- $m\angle 4 = m\angle 4$
- $\angle 5 = \angle 6$

- Symmetric property of equality
- Given
- Definition of linear angles
- Addition property of equality

Copy and complete the proof. Give the reason for the indicated step.

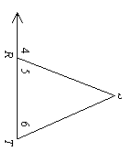


If $m\angle 4 + m\angle 6 = 180^\circ$, then $m\angle 5 = m\angle 6$.
Given: $m\angle 4 + m\angle 6 = 180^\circ$ Prove: $m\angle 5 = m\angle 6$

- $m\angle 4 + m\angle 6 = 180^\circ$
- $m\angle 4 + m\angle 5 = 180^\circ$
- $m\angle 4 + m\angle 5 = m\angle 4 + m\angle 6$
- $m\angle 4 = m\angle 4$
- $\angle 5 = \angle 6$

- Subtraction property of equality
- Symmetric property of equality
- Reflexive property of equality
- Addition property of equality

Copy and complete the proof. Give the reason for the indicated step.



If $m\angle 4 + m\angle 6 = 180^\circ$, then $m\angle 5 = m\angle 6$.
Given $m\angle 4 + m\angle 6 = 180^\circ$ Prove $m\angle 5 = m\angle 6$

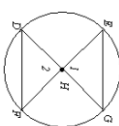
- $m\angle 4 + m\angle 6 = 180^\circ$
- $m\angle 4 + m\angle 5 = 180^\circ$
- $m\angle 4 + m\angle 5 = m\angle 4 + m\angle 6$
- $m\angle 4 = m\angle 6$

\Rightarrow e. $\underline{\hspace{1cm}} = \underline{\hspace{1cm}}$

- $m\angle 5 = m\angle 6$; Subtraction Property of equality
- $m\angle 4 = m\angle 6$; Given
- $m\angle 4 = m\angle 5$; Given
- $m\angle 4 = m\angle 5 = m\angle 6$; Reflexive property of equality

Write a two-column proof. Give a reason for the indicated step.

Given Circle H; arc $\overline{EG} \cong \text{arc } \overline{DF}$
Prove $\overline{EG} \cong \overline{DF}$

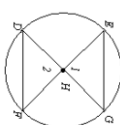


Proof

- arc $\overline{EG} \cong \text{arc } \overline{DF}$
 - $\overline{HE} \cong \overline{HD}$ and $\overline{HG} \cong \overline{HF}$
 - $\angle 1 \cong \angle 2$
 - $\triangle EHG \cong \triangle DHF$
 - $\overline{EG} \cong \overline{DF}$
- Congruent arcs have congruent chords.
 - Corresponding central angles to congruent arcs are congruent.
 - Minor arcs are congruent.
 - Linear pairs of angles are congruent.

Write a two-column proof. Give a reason for the indicated step.

Given Circle H; arc $\overline{EG} \cong \text{arc } \overline{DF}$
Prove $\overline{EG} \cong \overline{DF}$



Proof

- arc $\overline{EG} \cong \text{arc } \overline{DF}$
 - $\overline{HE} \cong \overline{HD}$ and $\overline{HG} \cong \overline{HF}$
 - $\angle 1 \cong \angle 2$
 - $\triangle EHG \cong \triangle DHF$
 - $\overline{EG} \cong \overline{DF}$
- All diameters of a circle are congruent.
 - All radii of a circle are congruent.
 - Congruent arcs have congruent chords.
 - Chords are congruent.

Write a two-column proof. Give a reason for the indicated step.

Given Circle H; arc $\overline{EG} \cong \text{arc } \overline{DF}$
Prove $\overline{EG} \cong \overline{DF}$



Proof

- arc $\overline{EG} \cong \text{arc } \overline{DF}$
 - $\overline{HE} \cong \overline{HD}$ and $\overline{HG} \cong \overline{HF}$
 - $\angle 1 \cong \angle 2$
 - $\triangle EHG \cong \triangle DHF$
 - $\overline{EG} \cong \overline{DF}$
- SSS
 - ASA