Name: \_\_\_\_\_ Date: \_\_\_\_\_

ID: A

## **Two-Column Proofs**

# **Multiple Choice**

*Identify the choice that best completes the statement or answers the question.* 

Complete the proof by giving the reason for the indicated step.

If 
$$\frac{2}{3}x = 8 - 2x$$
, then  $x = 3$ .

Given: 
$$\frac{2}{3}x = 8 - 2x$$
 Prove:  $x = 3$ 

\_\_\_\_ 1.

1. a. 
$$\frac{2}{3}x = 8 - 2x$$

$$\Rightarrow$$
 b.  $2x = 3(8 - 2x)$ 

c. 
$$2x = 24 - 6x$$

d. 
$$8x = 24$$

e. 
$$x = 3$$

- a. Multiplication property of equality
- b. Division property of equality
- c. Addition property of equality
- d. Reflexive property of equality

2.

a. 
$$\frac{2}{3}x = 8 - 2x$$

b. 
$$2x = 3(8 - 2x)$$

c. 
$$2x = 24 - 6x$$

$$\Rightarrow$$
 d.  $8x = 24$ 

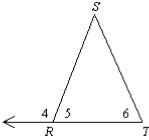
e. 
$$x = 3$$

- a. Subtraction property of equality
- b. Addition property of equality
- c. Substitution property of equality
- d. Symmetric property of equality

Name: \_\_\_\_\_

ID: A

Copy and complete the proof. Give the reason for the indicated step.



If  $m \angle 4 + m \angle 6 = 180^{\circ}$ , then  $m \angle 5 = m \angle 6$ .

Given:  $m \angle 4 + m \angle 6 = 180^{\circ}$ 

Prove:  $m \angle 5 = m \angle 6$ 

- 3.  $\Rightarrow$  a.  $m \angle 4 + m \angle 6 = 180^{\circ}$ 
  - b.  $m \angle 4 + m \angle 5 = 180^{\circ}$
  - c.  $m \angle 4 + m \angle 5 = m \angle 4 + m \angle 6$
  - d.  $m \angle 4 = m \angle 4$
  - e. <u>?</u> = <u>?</u>
  - a. Symmetric property of equality
  - b. Addition property of equality
  - c. Given
  - d. Definition of linear angles

4. a. 
$$m \angle 4 + m \angle 6 = 180^{\circ}$$

b. 
$$m \angle 4 + m \angle 5 = 180^{\circ}$$

$$\Rightarrow$$
 c.  $m \angle 4 + m \angle 5 = m \angle 4 + m \angle 6$ 

d. 
$$m \angle 4 = m \angle 4$$

e. 
$$? = ?$$

- a. Reflexive property of equality
- b. Given
- c. Addition property of equality
- d. Substitution property of equality

5. a. 
$$m \angle 4 + m \angle 6 = 180^{\circ}$$

b. 
$$m \angle 4 + m \angle 5 = 180^{\circ}$$

c. 
$$m \angle 4 + m \angle 5 = m \angle 4 + m \angle 6$$

d. 
$$m \angle 4 = m \angle 4$$

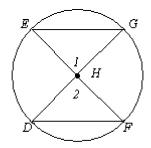
a. 
$$m \angle 4 = m \angle 5$$
; Given

- b.  $m \angle 4 = m \angle 5 = m \angle 6$ ; Reflexive property of equality
- c.  $m \angle 4 = m \angle 6$ ; Given
- d.  $m \angle 5 = m \angle 6$ ; Subtraction Property of equality

Write a two-column proof. Give a reason for the indicated step.

Given: Circle H; arc  $EG \cong arc DF$ 

Prove:  $\overline{EG} \cong \overline{DF}$ 



#### 6. Proof:

a. arc  $EG \cong \operatorname{arc} DF$ 

$$\Rightarrow$$
 b.  $\overline{HE} \cong \overline{HD}$  and  $\overline{HG} \cong \overline{HF}$ 

c. 
$$\angle 1 \cong \angle 2$$

d. 
$$\Delta EHG \cong \Delta DHF$$

e. 
$$\overline{EG} \cong \overline{DF}$$

a. Congruent arcs have congruent chords.

b. Chords are congruent.

c. All diameters of a circle are congruent.

d. All radii of a circle are congruent.

### 7. Proof:

a.  $\operatorname{arc} EG \cong \operatorname{arc} DF$ 

b. 
$$HE \cong HD$$
 and  $HG \cong HF$ 

c. 
$$\angle 1 \cong \angle 2$$

 $\Rightarrow$  d.  $\triangle EHG \cong \triangle DHF$ 

e. 
$$\overline{EG} \cong \overline{DF}$$

a. SSS

b. SAS

c. AA

d. ASA

# **Two-Column Proofs Answer Section**

### **MULTIPLE CHOICE**

- 1. A
- 2. B
- 3. C
- 4. D
- 5. D
- 6. D
- 7. B

